

A Program Logic for Tree Borrows

Johannes Hostert¹, Ralf Jung¹

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1: ETH Zurich, Switzerland

References Forbid Aliasing

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fn foo(a: &mut i32) {  
    let x = *a;  
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Correctness: `bar()` can not access `a`,
since mutable references have no aliases... or do they?

Unsafe Code Can Create Aliasing References

```
fn foo(a: &mut i32) { .. }

static mut GLOBAL: i32 = 0;
fn bar() {
    unsafe { println!("{}", &GLOBAL); }
}
fn main() {
    let a = unsafe { &mut GLOBAL };
    foo(a);
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Without optimizations:

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Without optimizations:

~> 42

With optimizations:

~> 0

Why Is This Optimization Legal?

Idea: Declare that our `unsafe` code is wrong!

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41

Stacked Borrows: An Aliasing Model for Rust

RALF JUNG, Mozilla, USA and MPI-SWS, Germany

HOANG-HAI DANG, MPI-SWS, Germany

JEEHOON KANG, KAIST, Korea

DEREK DREYER, MPI-SWS, Germany

Type systems are useful not just for the safety guarantees they provide, but also for helping compilers generate more efficient code by simplifying important program analyses. In Rust, the type system imposes a strict discipline on pointer aliasing, and it is an express goal of the Rust compiler developers to make use of that disci-

Why Is This Optimization Legal?

Idea: Declare that our `unsafe` code is wrong!



Tree Borrows

NEVEN VILLANI*, Univ. Grenoble Alpes, CNRS, Grenoble INP (Institute of Engineering), France

JOHANNES HOSTERT*, ETH Zurich, Switzerland

DEREK DREYER, MPI-SWS, Germany

RALF JUNG†, ETH Zurich, Switzerland

The Rust programming language is well known for its ownership-based type system, which offers strong guarantees like memory safety and data race freedom. However, Rust also provides *unsafe* escape hatches, for which safety is not guaranteed automatically and must instead be manually upheld by the programmer. This is not a problem if the programmer is diligent and upholds the safety invariants. But what if the programmer is not?

What is Tree Borrows?

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Wrongly aliased references are defined to **have UB!**
change Operational Semantics

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less UB



more UB

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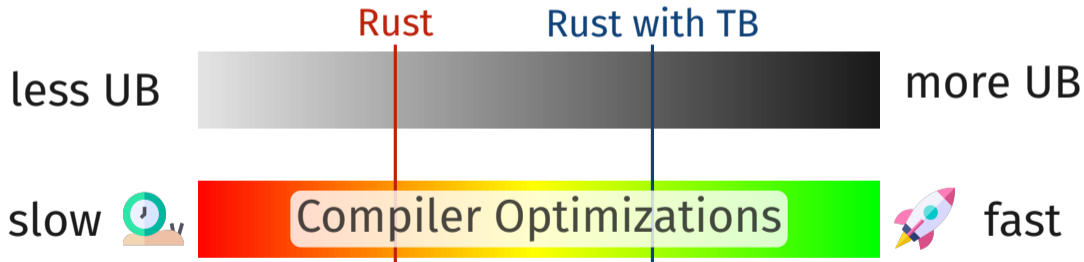
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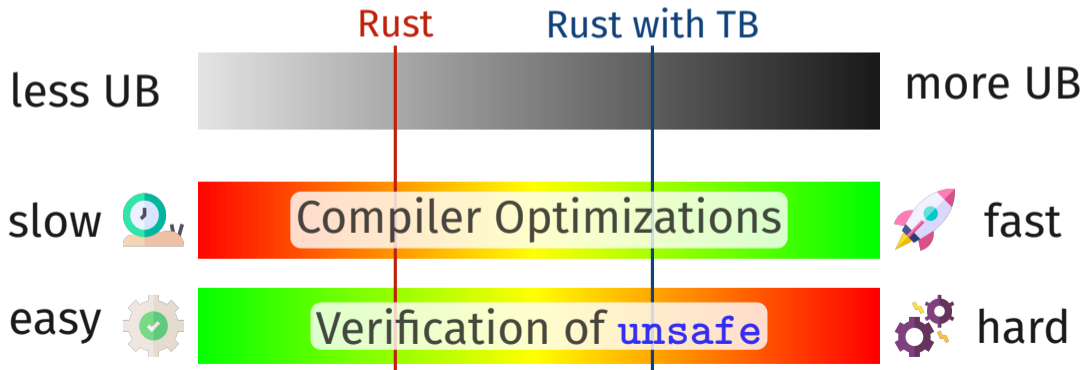
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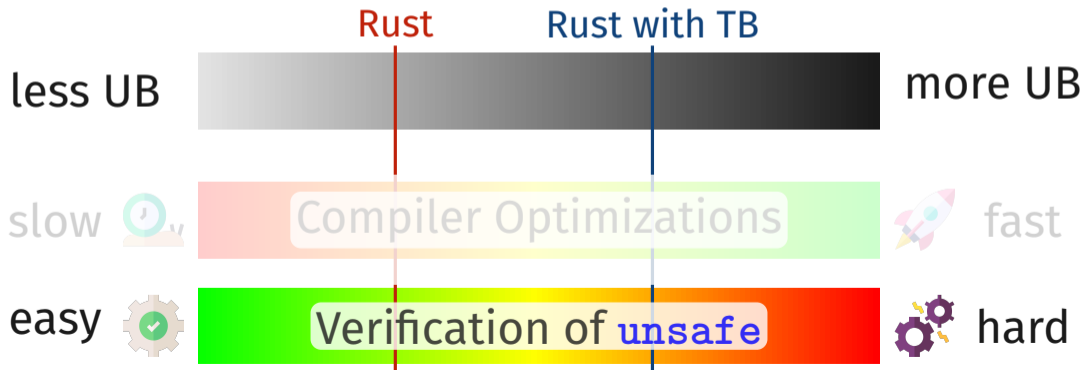
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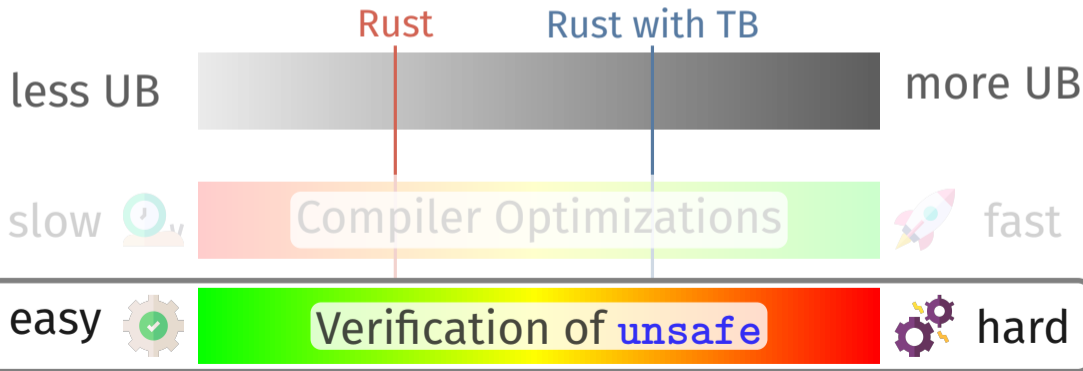
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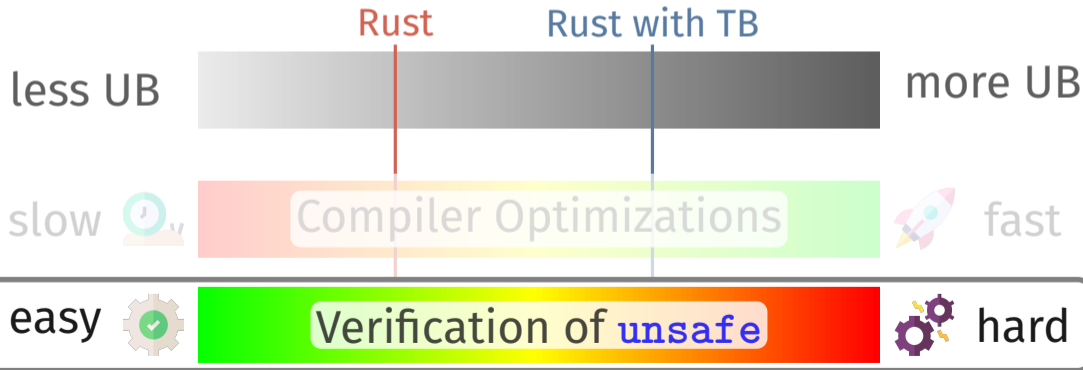
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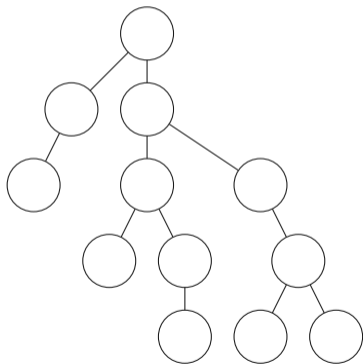


Putting The Borrows Into Trees

Tree Borrows tracks references in a tree data structure:

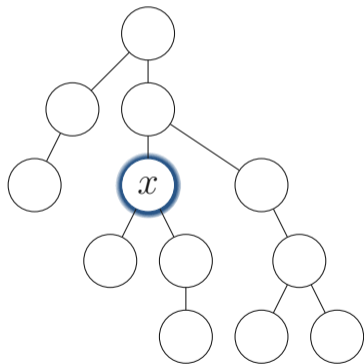
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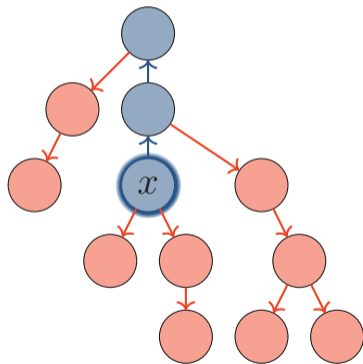
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One tree for each memory location.

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Nodes precisely represent references.
One tree for each memory location.

Each access to x splits tree in two:

- **Local:** references x is reborrowed from
- **Foreign:** references unrelated to x

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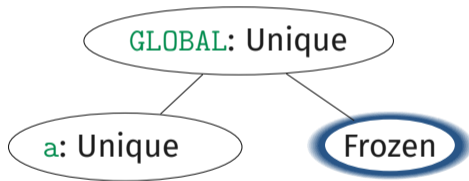


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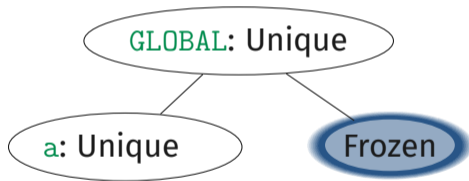


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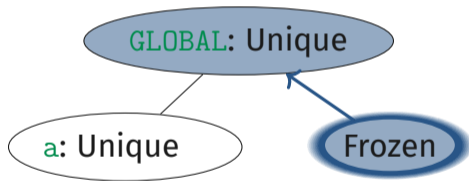
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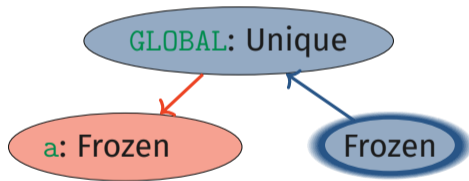
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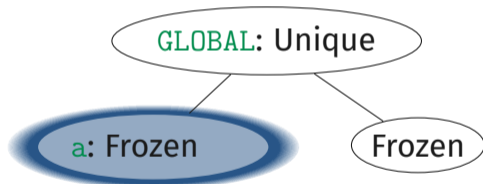


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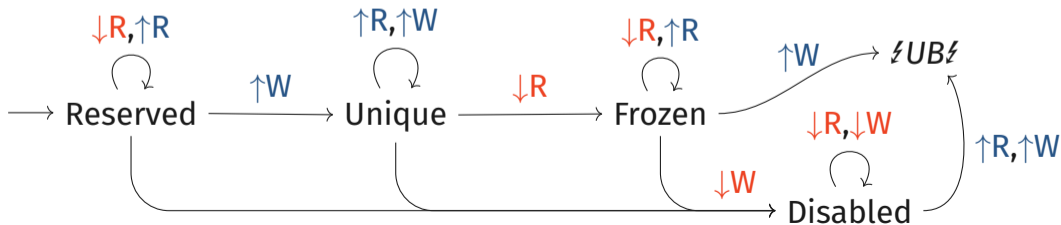
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States represent permissions to read or write.

Every access causes transitions at every node, based on

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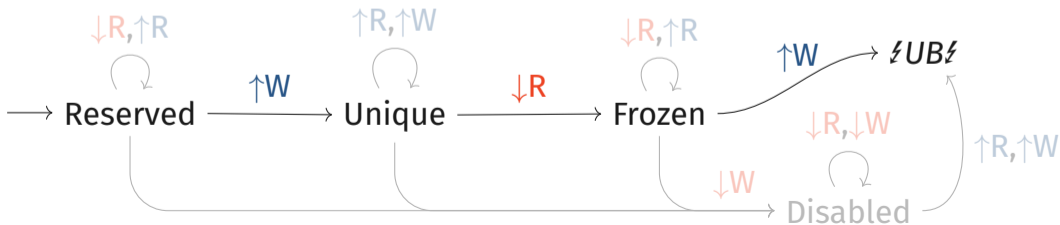


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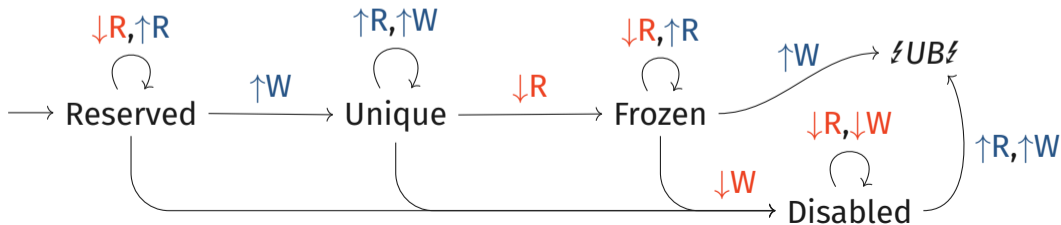


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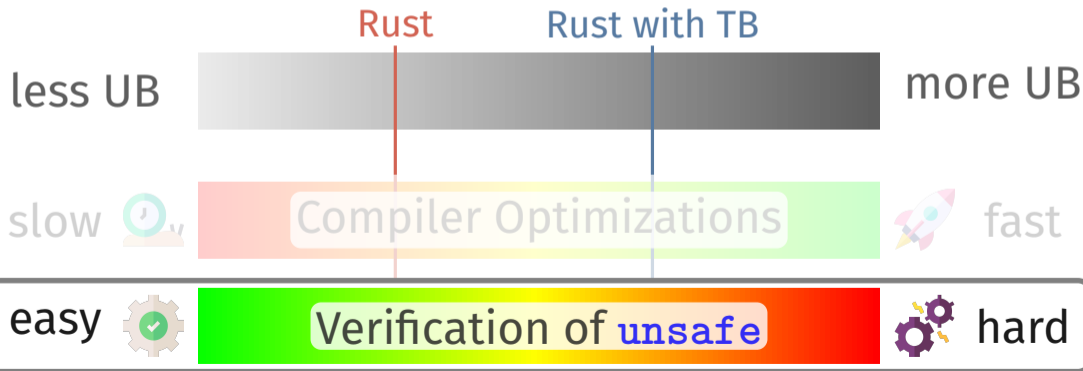
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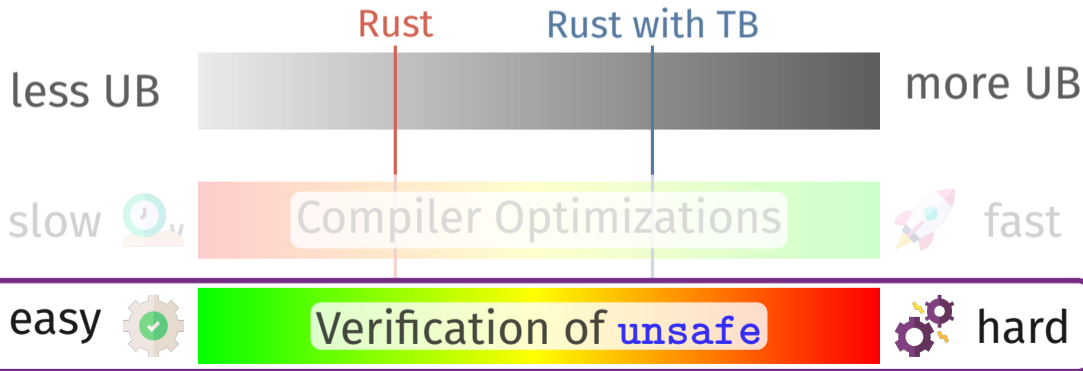
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Separation Logic

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Full Tree Details

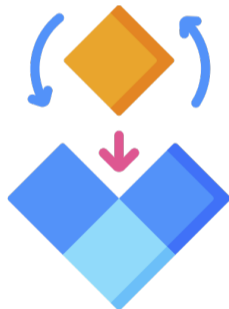
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Modular Reasoning

The Solution: A Program Logic for Tree Borrows

Theory at the Foundation of unsafe Verification Tools

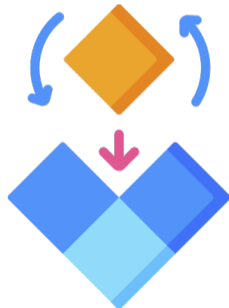
Prusti, GillianRust, Verifast, Verus, ...



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Modular Reasoning

A (Classical) Separation Logic Refresher

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$\forall z_1, z_2. \{x \mapsto z_1 * y \mapsto z_2\}$

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A (Classical) Separation Logic Refresher

?? Describes the Tree Borrows state

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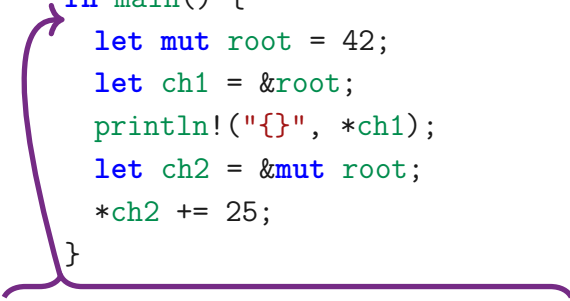
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Resources in Action

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    let mut root = 42;  
    let ch1 = &root;  
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    let ch2 = &mut root;  
    *ch2 += 25;  
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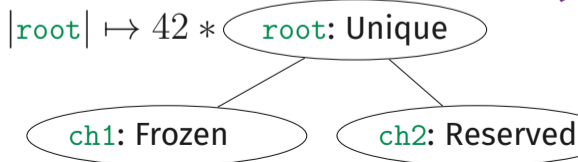
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ch1: Frozen

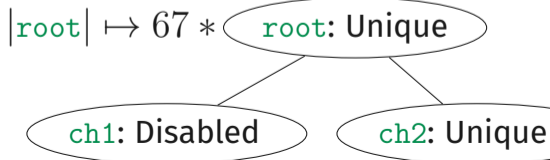
Resources in Action

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fn main() {  
    let mut root = 42;  
    let ch1 = &root;  
    println!("{}", *ch1);  
    let ch2 = &mut root;  
    *ch2 += 25;  
}
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```

```
fn incr(r : &mut i32) {  
    *r += 25;  
}
```

$|root| \mapsto 67 * \text{root: Unique}$

ch1: Disabled

ch2: Unique

Abstraction

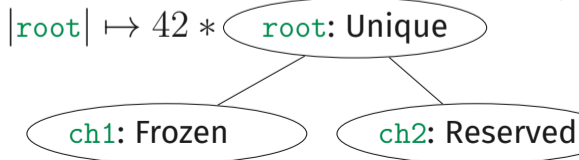
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  incr(ch2);  
}
```

$\{|r| \mapsto 42 * \text{ch2: Reserved}\}$

```
fn incr(r : &mut i32) {  
  *r += 25;  
}
```

$\{|r| \mapsto 67 * \text{ch2: Unique}\}$

$|root| \mapsto 42 * \text{root: Unique}$

ch1: Frozen

ch2: _____

Abstraction

```
fn main() {  
  let mut root = 42;  
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  println!("{}", *ch1);  
  let ch2 = &mut root;  
  incr(ch2);  
}
```

$\{|r| \mapsto 42 * \text{ch2: Reserved}\}$

```
fn incr(r : &mut i32) {  
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```

$\{|r| \mapsto 67 * \text{ch2: Unique}\}$

$|root| \mapsto 67 * \text{root: Unique}$

ch1: Frozen

ch2: Unique

Abstraction

```
fn main() {  
    let mut root = 42;  
    let ch1 = &root;  
    println!("{}", *ch1);  
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    incr(ch2);  
}
```

$\{|r| \mapsto 42 * \text{ch2: Reserved}\}$

```
fn incr(r : &mut i32) {  
    *r += 25;  
}
```

$\{|r| \mapsto 67 * \text{ch2: Unique}\}$

$|root| \mapsto 42 * \text{root: Unique}$

ch1: Frozen

ch2: _____

Abstraction

```
fn main() {  
    let mut root = 42;  
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}
```

$|root| \mapsto 42 * \text{root: Unique}$

$ch1: \text{Frozen}$

$\uparrow W \quad \downarrow -$
 $ch2:$

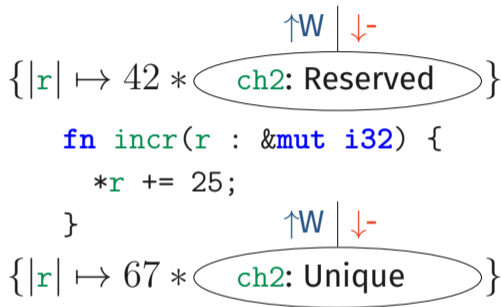
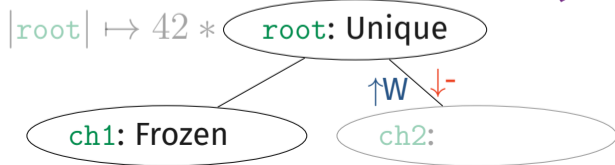
$\uparrow W \quad \downarrow -$
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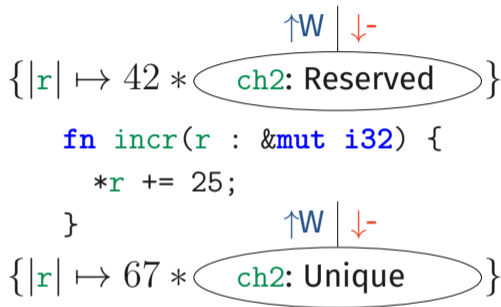
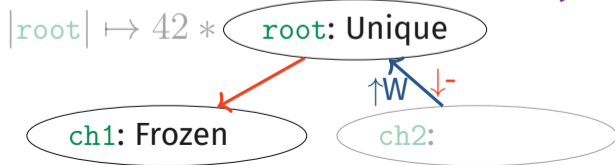


Protocol $\uparrow W \downarrow -$ imposes:

- ch2 can write
- Others may not access

Abstraction

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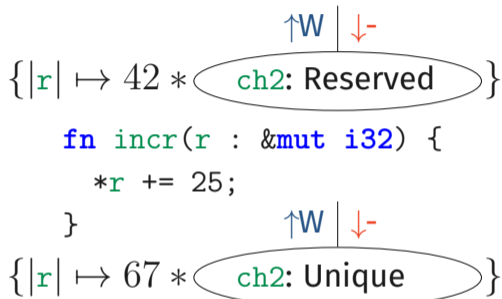
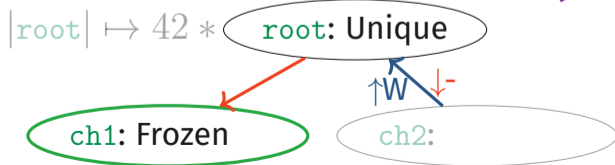


Protocol $\uparrow W \downarrow -$ imposes:

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Abstraction

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}
```



Protocol $\uparrow W \downarrow -$ imposes:

- $ch2$ can write (Invariance)
- Others may not access

Abstraction

```
fn main() {  
  let mut root = 42;  
  let ch1 = &root;  
  println!("{}", *ch1);  
  let ch2 = &mut root;  
  incr(ch2);  
}
```

$|root| \mapsto 42 * \text{root: Unique}$

$ch1: \text{Disabled}$

$ch2:$

$\uparrow W \mid \downarrow -$

$\{|r| \mapsto 42 * \text{ch2: Reserved}\}$

```
fn incr(r : &mut i32) {  
  *r += 25;  
}
```

$\uparrow W \mid \downarrow -$

$\{|r| \mapsto 67 * \text{ch2: Unique}\}$

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```
fn main() {  
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}
```

$|root| \mapsto 42 * \text{root: Unique}$

$ch1: \text{Disabled}$

$ch2:$

$\uparrow W \mid \downarrow -$
 $\{|r| \mapsto 42 * \text{ch2: Unique}\}$

```
fn incr(r : &mut i32) {  
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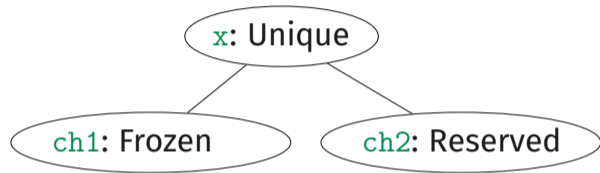
$\uparrow W \mid \downarrow -$
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Protocol $\uparrow W \downarrow -$ imposes:

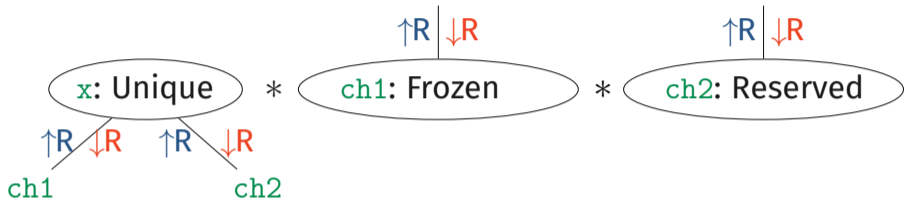
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Protocols + Invariance = Local Reasoning

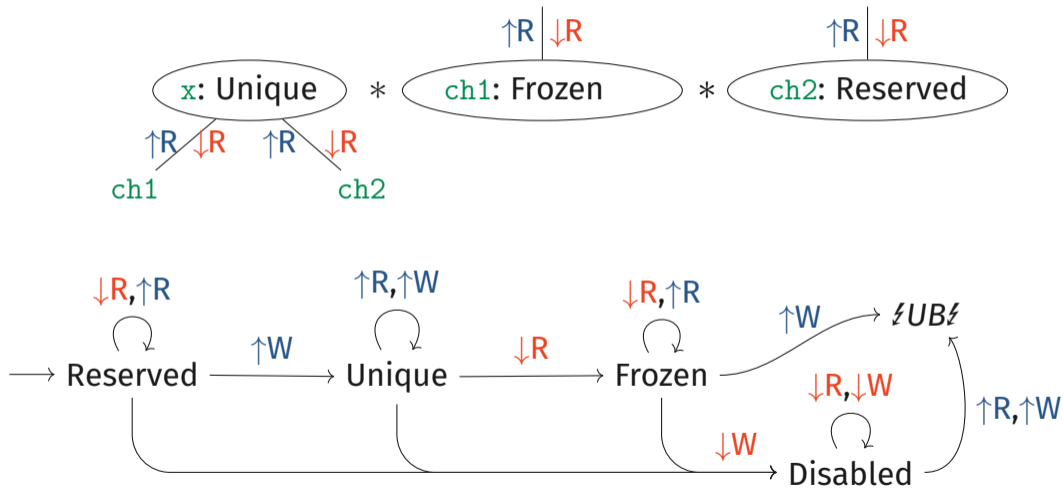
Protocols + Invariance = Local Reasoning



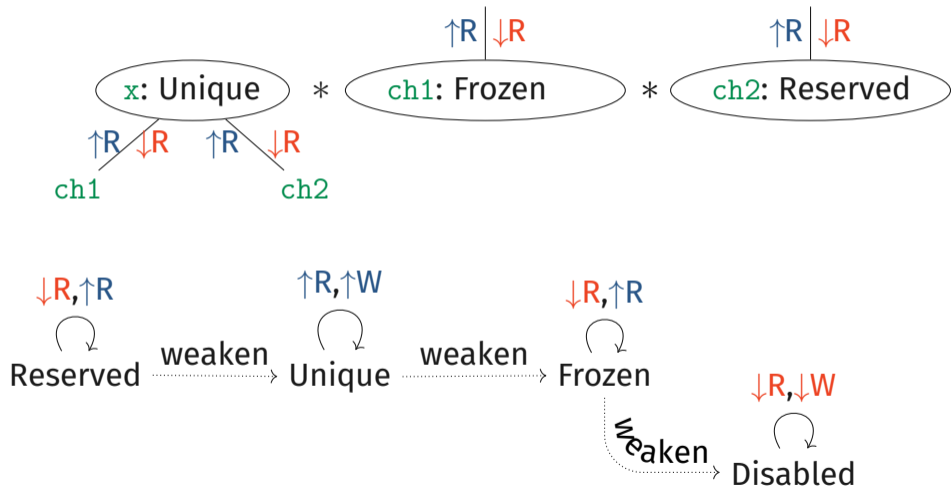
Protocols + Invariance = Local Reasoning



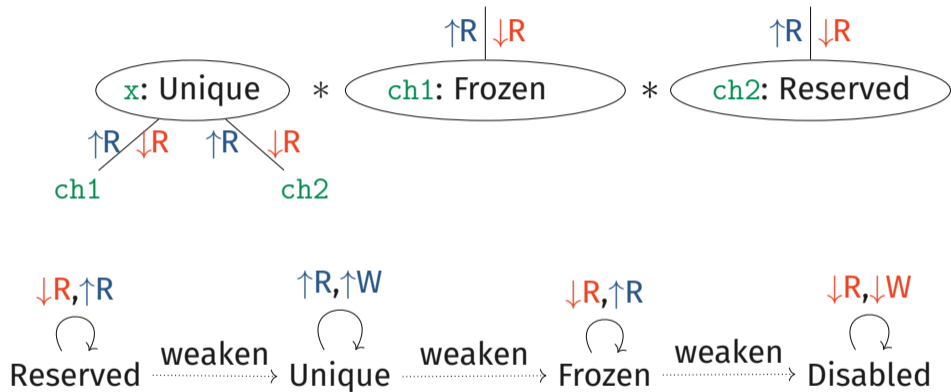
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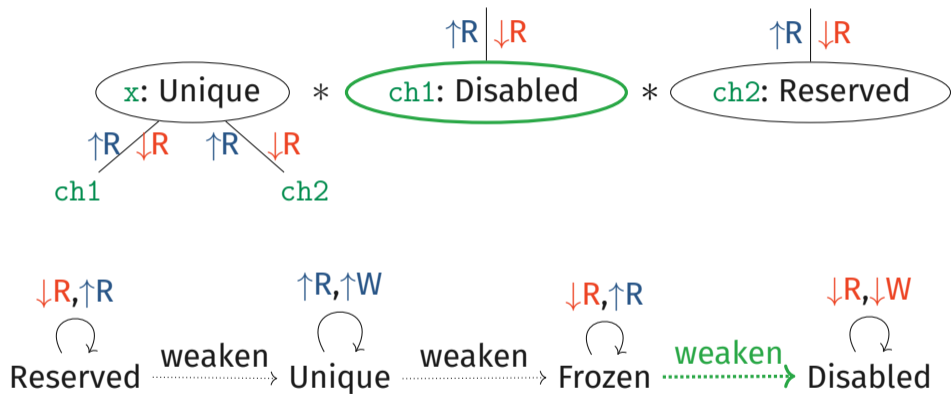
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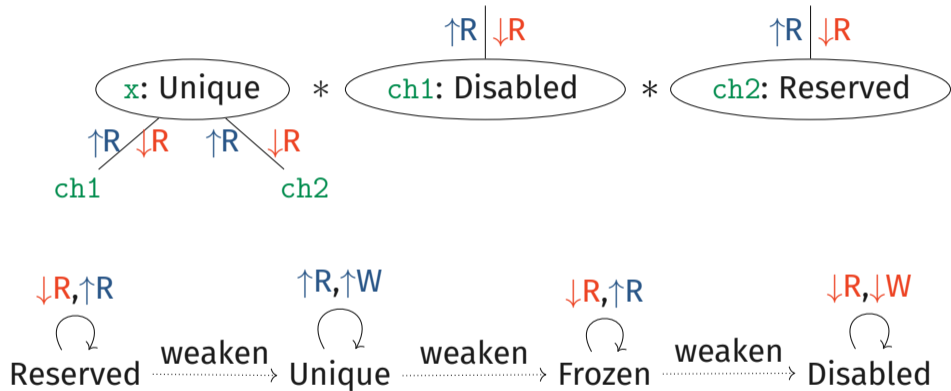
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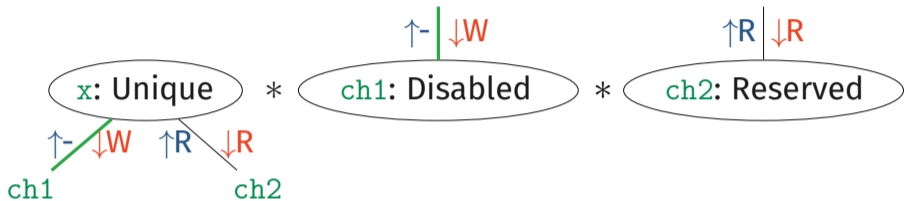


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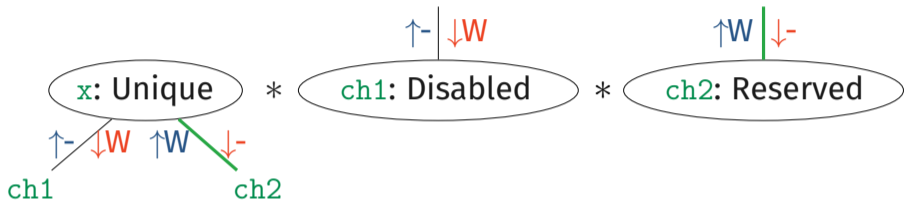
Protocol Compatibility: Nothing (-) \leq Read \leq Write

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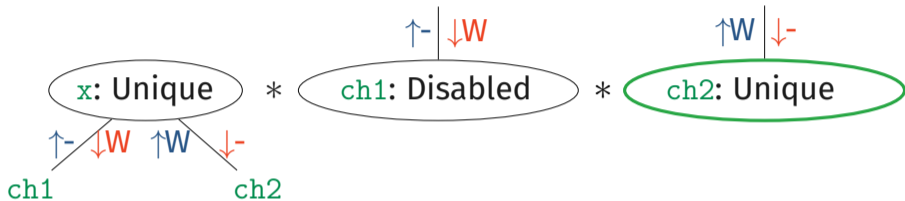
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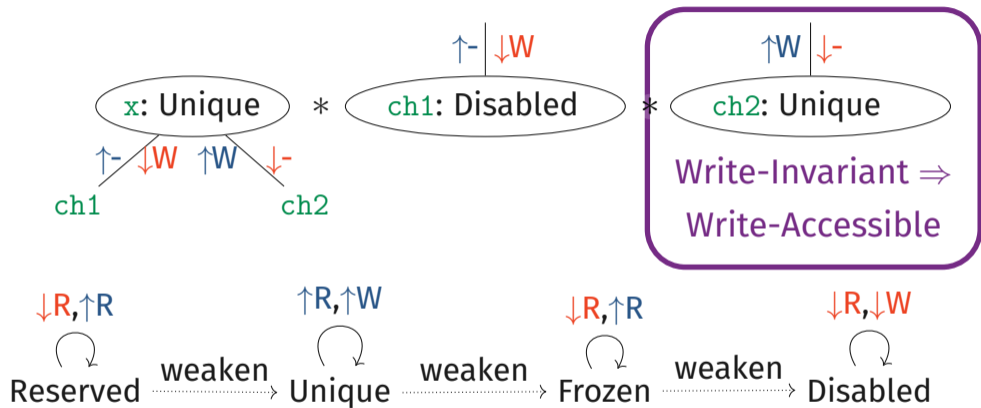
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Protocol Compatibility: Nothing (-) \leq Read \leq Write

This is Just the Beginning

Our logic can do much more:

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- Pointer Arithmetic (“Dynamic Ranges”)
- Interior Mutability, ReservedIM, ...

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- *all dark corners* of Tree Borrows

This is Just the Beginning



ROCQ
APPROVED

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Current Status: Iris implementation, small case-studies

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Current Status: Iris implementation, small case-studies

Further plans: More examples, simplification, completeness?, verifier integration?? ...

The End

Thanks for your attention!

What is Tree Borrows?

Wrongly aliased references are defined to have UB!
change Operational Semantics



Protocols + Invariance = Local Reasoning



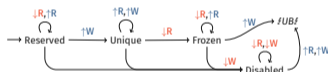
Protocol Compatibility: Nothing (-) ≤ Read (R) ≤ Write (W)

Each Node is a State Machine

States represent permissions to read or write.

Every access causes transitions at every node, based on

- Local (↑) vs. Foreign (↓) access
- Read (R) vs. Write (W) access



This is Just the Beginning



Our logic can do much more:

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More info:

